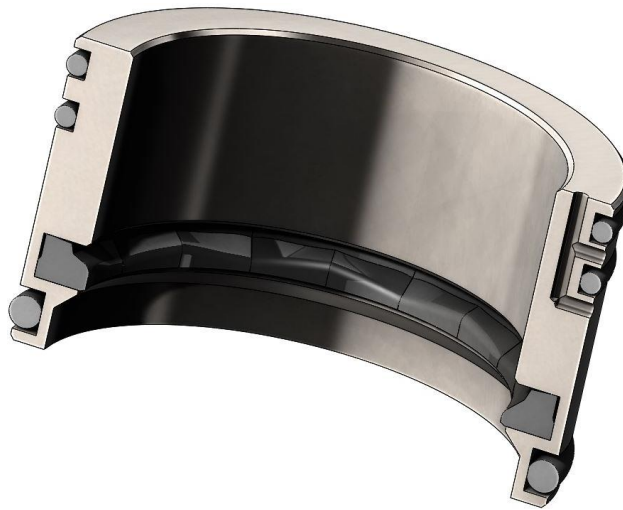


## Appendix 5

Example problem: Annular piston reservoir sizing

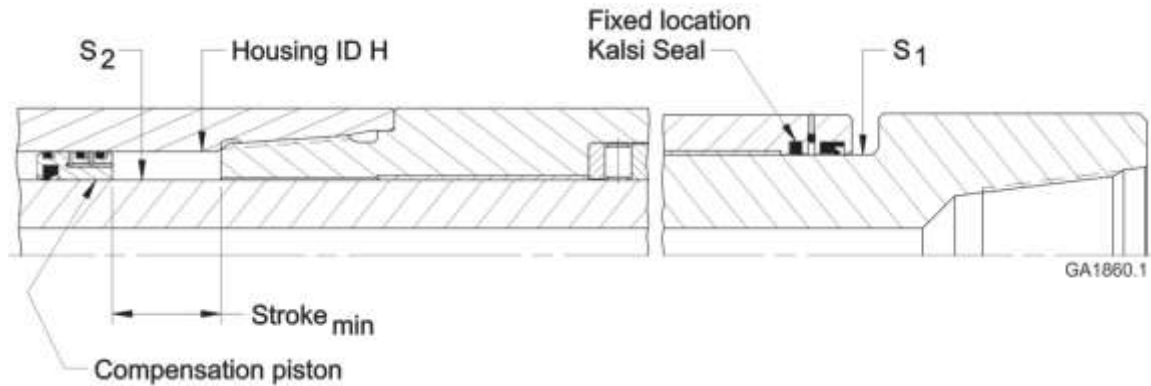


### Revision 3 December 9, 2015

Individual appendices of the Kalsi Seals Handbook are periodically updated. To determine if a newer revision of this appendix exists, please visit [www.kalsi.com/seal-handbook.htm](http://www.kalsi.com/seal-handbook.htm).

**NOTICE:** The information in this chapter is provided under the terms and conditions of the Offer of Sale, Disclaimer, and other notices provided in the front matter of this handbook.

**1. Example Problem: Calculate the minimum piston stroke length for a mud motor**



**Figure 1**

**Schematic of a typical oilfield sealed bearing downhole drilling mud motor**

- GIVEN:** Maximum Rotary Speed: 480 RPM  
 Fixed location Seal ID ( $S_1$ ): 4.00”  
 Compensation piston Seal ID ( $S_2$ ): 3.25”  
 Lubricant Viscosity: ISO 680 VG  
 $Y = 2.056 \times 10^{-4}$  (per Chapter C3)  
 Tool Life: 200 hrs  
 Housing ID ( $H$ ): 6.50”  
 Tool lubricant volume: 173.25 in<sup>3</sup>  
 Assume lubricant volumetric thermal expansion of 10%

**FIND:** Minimum piston stroke length ( $Stroke_{min}$ ).

**SOLUTION:**

(a) Calculate lubricant volume pumping rate,  $Q_2$ , for Compensation Piston seal.

$$Q_2 = Y \times S_2^2 \times V_{rpm}$$

$$Q_2 = 2.056 \times 10^{-4} \times 3.25''^2 \times 480 \text{ RPM}$$

$$Q_2 = 1.04 \text{ ml/hr}$$

(b) Calculate lubricant volume pumping rate,  $Q_1$ , for Fixed location Seal.

$$Q_1 = Y \times S_1^2 \times V_{rpm}$$

$$Q_1 = 2.056 \times 10^{-4} \times 4.00''^2 \times 480 \text{ RPM}$$

$$Q_1 = 1.58 \text{ ml/hr}$$

(c) Calculate total lubricant volume pumping rate,  $Q_{total}$ , for both Kalsi Seals.

$$Q_{total} = Q_1 + Q_2$$

$$Q_{\text{total}} = 1.04 \text{ ml/hr} + 1.58 \text{ ml/hr}$$

$$Q_{\text{total}} = 2.62 \text{ ml/hr}$$

- (d) Calculate the total required lubricant volume,  $\text{Vol}_{\text{lub}}$ , for tool service life.

$$\text{Vol}_{\text{lub}} = Q \times \text{Tool Life}$$

$$\text{Vol}_{\text{lub}} = 2.62 \text{ ml/hr} \times 200 \text{ hrs}$$

$$\text{Vol}_{\text{lub}} = 524 \text{ ml or } 31.97 \text{ in}^3$$

- (e) Calculate piston stroke length,  $\text{Stroke}_{\text{SL}}$ , for tool service life.

$$\text{Stroke}_{\text{SL}} = \text{Volume}_{\text{lub}} / \text{Annular Area}$$

$$\text{Stroke}_{\text{SL}} = \text{Volume}_{\text{lub}} / ((H^2 - S_1^2) \times \text{PI} / 4)$$

$$\text{Stroke}_{\text{SL}} = 31.97 \text{ in}^3 / ((6.50''^2 - 4.00''^2) \times \text{PI} / 4)$$

$$\text{Stroke}_{\text{SL}} = 1.55''$$

Calculate piston stroke length,  $\text{Stroke}_{\text{TE}}$ , required for thermal expansion of lubricant.

$$\text{Stroke}_{\text{TE}} = (\text{Vol}_{\text{tool}} + \text{Vol}_{\text{lub}}) \times 10\% / ((H^2 - \text{Shaft OD}^2) \times \text{PI} / 4)$$

$$\text{Stroke}_{\text{TE}} = (173.25 \text{ in}^3 + 31.97 \text{ in}^3 \times 10\%) / ((6.50''^2 - 4.00''^2) \times \text{PI} / 4)$$

$$\text{Stroke}_{\text{TE}} = 1.00''$$

- (f) Calculate total minimum piston stroke length  $\text{Stroke}_{\text{min}}$ .

$$\text{Stroke}_{\text{min}} = \text{Stroke}_{\text{SL}} + \text{Stroke}_{\text{TE}}$$

$$\text{Stroke}_{\text{min}} = 1.55'' + 1.00''$$

$$\text{Stroke}_{\text{min}} = 2.55''$$